## Vector Space Model

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## The Search Task

- Given a query and a corpus, find relevant items query: a textual description of the user's information need corpus: a repository of textual documents relevance: satisfaction of the user's information need


## What is a Retrieval Model?

- A formal method that predicts the degree of relevance of a document to a query


## Basic Information Retrieval Process



## Boolean Retrieval Models

- The user describes their information need using boolean constraints (e.g., AND, OR, and AND NOT)
- Unranked Boolean: retrieves documents that satisfy the constraints in no particular order
- Ranked Boolean: retrieves documents that satisfy the constraints and orders them based on the number of ways they satisfy the constraints
- Also known as 'exact-match' retrieval models
- Advantages and disadvantages?


## Boolean Retrieval Models

- Advantages:
- Easy for the system
- Users get transparency: it is easy to understand why a document was or was not retrieved
- Users get control: it is easy to determine whether the query is too specific (few results) or too broad (many results)
- Disadvantages:
- The burden is on the user to formulate an effective query


## Relevance

- Many factors affect whether a document satisfies a particular user's information need
- Topicality, freshness, authority, formatting, reading level, assumed level of prior knowledge/expertise, novelty...
- Topical relevance: the document is on the same topic as the query
- User relevance: everything else!
- For now, we will only try to predict topical relevance


## Introduction to Best-Match Retrieval Models

- Best-match models predict the degree to which a document is relevant to a query
- Ideally, this would be expressed as RELEVANT(q,d)
- In practice, it is expressed as $\operatorname{SIMILAR}(\mathbf{q}, \mathrm{d})$


## Vector Space Model

## What is a Vector Space?

- Formally, a vector space is defined by a set of linearly independent basis vectors
- The basis vectors correspond to the dimensions or directions of the vector space



## What is a Vector?

- A vector is a point in a vector space and has length (from the origin to the point) and direction




## What is a Vector?

- A 2-dimensional vector can be written as [x,y]
- A 3-dimensional vector can be written as $[x, y, z]$




## What is a Vector Space?

- The basis vectors are linearly independent because knowing a vector's value along one dimension doesn't say anything about its value along another dimension

basis vectors for 2dimensional space



## Binary Text Representation

|  | $a$ | aardvark | abacus | abba | able | ... | zoom |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| doc_l | 1 | 0 | 0 | 0 | 0 | $\ldots$ | I |
| doc_2 | 0 | 0 | 0 | 0 | 1 | $\ldots$ | I |
| :: | $::$ | $::$ | $::$ | $::$ | $::$ | $\ldots$ | 0 |
| doc_m | 0 | 0 | $I$ | $I$ | 0 | $\ldots$ | 0 |

- $1=$ the word appears in the document
- $0=$ the word does not appear in the document
- Does not represent word frequency, word location, or word order information


## Vector Space Representation

- Let V denote the size of the indexed vocabulary
- $\mathrm{V}=$ the number of unique terms,
- $\mathrm{V}=$ the number of unique terms excluding stopwords,
- $\mathrm{V}=$ the number of unique stems, etc...
- Any arbitrary span of text (i.e., a document, or a query) can be represented as a vector in V-dimensional space
- For simplicity, let's assume three index terms: dog, bite, man (i.e., $V=3$ )
- Why? Because it's easy to visualize 3-D space


## Vector Space Representation with binary weights

- $1=$ the term appears at least once
- $0=$ the term does not appear



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## Vector Space Representation with binary weights

- What span(s) of text does this vector represent?



## Vector Space Representation with binary weights

- What span(s) of text does this vector represent?



## Vector Space Representation with binary weights

- What span(s) of text does this vector represent?



## Vector Space Representation

- Any span of text is a vector in V-dimensional space, where V is the size of the vocabulary



## Vector Space Representation

- A query is a vector in V-dimensional space, where V is the number of terms in the vocabulary



## Vector Space Similarity

- The vector space model ranks documents based on the vector-space similarity between the query vector and the document vector
- There are many ways to compute the similarity between two vectors
- One way is to compute the inner product

$$
\sum_{i=1}^{V} x_{i} \times y_{i}
$$

## The Inner Product

- Multiply
corresponding components and then sum those products

$$
\sum_{i=1}^{V} x_{i} \times y_{i}
$$

|  | $x_{i}$ | $y_{i}$ | $x_{i} \times y_{i}$ |
| :---: | :---: | :---: | :---: |
| $a$ | 1 | 1 | 1 |
| aardvark | 0 | 1 | 0 |
| abacus | 1 | 1 | 1 |
| abba | 1 | 0 | 0 |
| able | 0 | 1 | 0 |
| $::$ | 0 | 0 | 0 |
| zoom | 0 | 0 | 0 |
| inner product $=>$ |  |  |  | 2.

## The Inner Product

- What does the inner product (with a binary representation) correspond to?

$$
\sum_{i=1}^{V} x_{i} \times y_{i}
$$

| $a$ | 1 | 1 | 1 |
| :---: | :---: | :---: | :---: |
| aardvark | 0 | 1 | 0 |
| abacus | 1 | 1 | 1 |
| abba | 1 | 0 | 0 |
| able | 0 | 1 | 0 |
| $::$ | 0 | 0 | 0 |
| zoom | 0 | 0 | 0 |
| inner product $=>$ |  |  |  |

## The Inner Product

- When using 0's and 1 's, this is just the number of unique terms in common between the query and the document

$$
\sum_{i=1}^{V} x_{i} \times y_{i}
$$

| $a$ | 1 | 1 | 1 |
| :---: | :---: | :---: | :---: |
| aardvark | 0 | 1 | 0 |
| abacus | 1 | 1 | 1 |
| $a b b a$ | 1 | 0 | 0 |
| able | 0 | 1 | 0 |
| $::$ | 0 | 0 | 0 |
| zoom | 0 | 0 | 0 |
| inner product $=>$ |  |  |  | 2.

## The Inner Product

- $1=$ the term appears at least once
- $0=$ the term does not appear

|  | dog | man | bite |
| :--- | :---: | :---: | :---: |
| doc_1 | 1 | 1 | 1 |
| doc_2 | 1 | 0 | 1 |
| doc_3 | 0 | 1 | 1 |
| doc_4 | 0 | 1 | 0 |



## The Inner Product

- Multiply corresponding components and then sum those products
- Using a binary representation, the inner product corresponds to the number of terms appearing (at least once) in both spans of text
- Scoring documents based on their inner-product with the query has one major issue. Any ideas?


## The Inner Product

- What is more relevant to a query?
- A 50-word document which contains 3 of the queryterms?
- A 100-word document which contains 3 of the query-terms?
- All things being equal, longer documents are more likely to have the query-terms
- The inner-product doesn't account for the fact that documents have widely varying lengths
- So, the inner-product favors long documents


## The Cosine Similarity

- The numerator is the inner product
- The denominator is the product of the two vector-lengths
- Ranges from 0 to 1 (equals 1 if the vectors are identical)
- The cosine of the angle between the two vectors
- 0 if the angle is 90 degrees

$$
\begin{aligned}
& \frac{\sum_{i=1}^{V} x_{i} \times y_{i}}{\sqrt{\sum_{i=1}^{V} x_{i}^{2}} \times \sqrt{\sum_{i=1}^{V} y_{i}^{2}}} \\
& \text { length of length of } \\
& \text { vector } \mathrm{x} \text { vector } \mathrm{y}
\end{aligned}
$$

## Vector Space Model

 cosine similarity example (binary weights)$$
\frac{\sum_{i=1}^{V} x_{i} \times y_{i}}{\sqrt{\sum_{i=1}^{V} x_{i}^{2}} \times \sqrt{\sum_{i=1}^{V} y_{i}^{2}}}
$$

cosine( $[I, 0, l],[I, I, 0])=$

$$
\frac{(1 \times 1)+(0 \times 1)+(1 \times 0)}{\sqrt{1^{2}+0^{2}+1^{2}} \times \sqrt{1^{2}+1^{2}+0^{2}}}=0.5
$$

$\frac{\sum_{i=1}^{V} x_{i} \times y_{i}}{\sqrt{\sum_{i=1}^{V} x_{i}^{2} \times \sqrt{\sum_{i=1}^{V} y_{i}^{2}}}}$ In Class Exercise

- For each document, compute the inner-product and cosine similarity score for the query: jill
doc_I Jack and jill went up the hill doc_2 To fetch a pail of water. doc_3 Jack fell down and broke his crown, doc_4 And Jill came tumbling after. doc_5 Up Jack got, and home did trot, doc_6 As fast as he could caper, doc_7 To old Dame Dob, who patched his nob doc_8 With vinegar and brown paper.
$\frac{\sum_{i=1}^{V} x_{i} \times y_{i}}{\sqrt{\sum_{i=1}^{V} x_{i}^{2} \times \sqrt{\sum_{i=1}^{V} y_{i}^{2}}}}$ In Class Exercise
- For each document, compute the inner-product and cosine similarity score for the query: Jack
doc_I Jack and jill went up the hill doc_2 To fetch a pail of water. doc_3 Jack fell down and broke his crown, doc_4 And jill came tumbling after. doc_5 Up Jack got, and home did trot, doc_6 As fast as he could caper, doc_7 To old Dame Dob, who patched his nob doc_8 With vinegar and brown paper.


## Vector Space Representation

|  | $a$ | aardvark | abacus | $a b b a$ | able | ... | zoom |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| doc_l | I | 0 | 0 | 0 | 0 | ... | I |
| doc_2 | 0 | 0 | 0 | 0 | I | ... | I |
| : | :: | :: | :: | :: | :: | ... | 0 |
| doc_m | 0 | 0 | I | I | 0 | ... | 0 |
|  | $a$ | aardvark | abacus | $a b b a$ | able | ... | zoom |
| query | 0 | I | 0 | 0 | I | ... | I |

- So far, we've assumed binary vectors
- 0 's and 1 's indicate whether the term occurs (at least once) in the document/query
- Let's explore a more sophisticated representation


## - Movie: Rocky (1976)

- Plot:

Rocky Balboa is a struggling boxer trying to make the big time. Working in a meat factory in Philadelphia for a pittance, he also earns extra cash as a debt collector. When heavyweight champion Apollo Creed visits Philadelphia, his managers want to set up an exhibition match between Creed and a struggling boxer, touting the fight as a chance for a "nobody" to become a "somebody". The match is supposed to be easily won by Creed, but someone forgot to tell Rocky, who sees this as his only shot at the big time. Rocky Balboa is a small-time boxer who lives in an apartment in Philadelphia, Pennsylvania, and his career has so far not gotten off the canvas. Rocky earns a living by collecting debts for a loan shark named Gazzo, but Gazzo doesn't think Rocky has the viciousness it takes to beat up deadbeats. Rocky still boxes every once in a while to keep his boxing skills sharp, and his ex-trainer, Mickey, believes he could've made it to the top if he was willing to work for it. Rocky, goes to a pet store that sells pet supplies, and this is where he meets a young woman named Adrian, who is extremely shy, with no ability to talk to men. Rocky befriends her. Adrain later surprised Rocky with a dog from the pet shop that Rocky had befriended. Adrian's brother Paulie, who works for a meat packing company, is thrilled that someone has become interested in Adrian, and Adrian spends Thanksgiving with Rocky. Later, they go to Rocky's apartment, where Adrian explains that she has never been in a man's apartment before. Rocky sets her mind at ease, and they become lovers. Current world heavyweight boxing champion Apollo Creed comes up with the idea of giving an unknown a shot at the title. Apollo checks out the Philadelphia boxing scene, and chooses Rocky. Fight promoter Jergens gets things in gear, and Rocky starts training with Mickey. After a lot of training, Rocky is ready for the match, and he wants to prove that he can go the distance with Apollo. The 'Italian Stallion', Rocky Balboa, is an aspiring boxer in downtown Philadelphia. His one chance to make a better life for himself is through his boxing and Adrian, a girl who works in the local pet store. Through a publicity stunt, Rocky is set up to fight Apollo Creed, the current heavyweight champion who is already set to win. But Rocky really needs to triumph, against all the odds...

## Term-Frequency

how important is a term?

| rank | term | freq. | rank | term | freq. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | a | 22 | 16 | creed | 5 |
| 2 | rocky | 19 | 17 | philadelphia | 5 |
| 3 | to | 18 | 18 | has | 4 |
| 4 | the | 17 | 19 | pet | 4 |
| 5 | is | 11 | 20 | boxing | 4 |
| 6 | and | 10 | 21 | up | 4 |
| 7 | in | 10 | 22 | an | 4 |
| 8 | for | 7 | 23 | boxer | 4 |
| 9 | his | 7 | 24 | s | 3 |
| 10 | he | 6 | 25 | balboa | 3 |
| 11 | adrian | 6 | 26 | it | 3 |
| 12 | with | 6 | 27 | heavyweigh | 3 |
| 13 | who | 6 | 28 | champion | 3 |
| 14 | that | 5 | 29 | fight | 3 |
| 15 | apollo | 5 | 30 | become | 3 |

## Term-Frequency

how important is a term?

| rank | term | freq. | rank | term | freq. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | a | 22 | 16 | creed | 5 |
| 2 | rocky | 19 | 17 | philadelphia | 5 |
| 3 | to | 18 | 18 | has | 4 |
| 4 | the | 17 | 19 | pet | 4 |
| 5 | is | 11 | 20 | boxing | 4 |
| 6 | and | 10 | 21 | up | 4 |
| 7 | in | 10 | 22 | an | 4 |
| 8 | for | 7 | 23 | boxer | 4 |
| 9 | his | 7 | 24 | s | 3 |
| 10 | he | 6 | 25 | balboa | 3 |
| 11 | adrian | 6 | 26 | it | 3 |
| 12 | with | 6 | 27 | heavyweigh | 3 |
| 13 | who | 6 | 28 | champion | 3 |
| 14 | that | 5 | 29 | fight | 3 |
| 15 | apollo | 5 | 30 | become | 3 |

# Inverse Document Frequency (IDF) how important is a term? 

$$
i d f_{t}=\log \left(\frac{N}{d f_{t}}\right)
$$

- $N=$ number of documents in the collection
- $d f_{t}=$ number of documents in which term $t$ appears


## Inverse Document Frequency (IDF) how important is a term?

| rank | term | idf | rank | term | idf |
| :---: | :---: | :---: | :---: | :---: | :---: |
| I | doesn | 11.66 | 16 | creed | 6.84 |
| 2 | adrain | 10.96 | 17 | paulie | 6.82 |
| 3 | viciousness | 9.95 | 18 | packing | 6.81 |
| 4 | deadbeats | 9.86 | 19 | boxes | 6.75 |
| 5 | touting | 9.64 | 20 | forgot | 6.72 |
| 6 | jergens | 9.35 | 21 | ease | 6.53 |
| 7 | gazzo | 9.21 | 22 | thanksgivin | 6.52 |
| 8 | pittance | 9.05 | 23 | earns | 6.51 |
| 9 | balboa | 8.61 | 24 | pennsylvani | 6.50 |
| 10 | heavyweigh | 7.18 | 25 | promoter | 6.43 |
| 11 | stallion | 7.17 | 26 | befriended | 6.38 |
| 12 | canvas | 7.10 | 27 | exhibition | 6.31 |
| 13 | ve | 6.96 | 28 | collecting | 6.23 |
| 14 | managers | 6.88 | 29 | philadelphia | 6.19 |
| 15 | apollo | 6.84 | 30 | gear | 6.18 |

## TF.IDF <br> how important is a term?



## TF.IDF

$$
t f_{t} \times \log \left(\frac{N}{d f_{t}}\right)
$$

| term | tf | N | df | idf | tf.idf |
| :---: | :---: | :---: | :---: | :---: | :---: |
| rocky | I 9 | 23072 I | 1420 | 5.09 | 96.72 |
| philadelphia | 5 | 230721 | 473 | 6.19 | 30.95 |
| boxer | 4 | 230721 | 900 | 5.55 | 22.19 |
| fight | 3 | 230721 | 8170 | 3.34 | 10.02 |
| mickey | 2 | 230721 | 2621 | 4.48 | 8.96 |
| for | 7 | 230721 | 117137 | 0.68 | 4.75 |

## TF.IDF

how important is a term?

| rank | term | tf.idf | rank | term | tf.idf |
| :---: | :---: | :---: | :---: | :---: | :---: |
| I | rocky | 96.72 | 16 | meat | 11.76 |
| 2 | apollo | 34.20 | 17 | doesn | 11.66 |
| 3 | creed | 34.18 | 18 | adrain | 10.96 |
| 4 | philadelphia | 30.95 | 19 | fight | 10.02 |
| 5 | adrian | 26.44 | 20 | viciousness | 9.95 |
| 6 | balboa | 25.83 | 21 | deadbeats | 9.86 |
| 7 | boxing | 22.37 | 22 | touting | 9.64 |
| 8 | boxer | 22.19 | 23 | current | 9.57 |
| 9 | heavyweigh | 21.54 | 24 | jergens | 9.35 |
| I0 | pet | 21.17 | 25 | s | 9.29 |
| II | gazzo | 18.43 | 26 | struggling | 9.21 |
| I2 | champion | 15.08 | 27 | training | 9.17 |
| I3 | match | 13.96 | 28 | pittance | 9.05 |
| 14 | earns | 13.01 | 29 | become | 8.96 |
| I5 | apartment | 11.82 | 30 | mickey | 8.96 |

## TF, IDF, or TF.IDF?

${ }_{\text {adain }}$ adrian ${ }_{\text {all aready aso }}$ an and apartment apollo as aspprine $a t$ balboa become beter big boxer boxing but by can career champion

 make man match meat men mickey named nobosy of puwe pet philadel phia rOCKY set sto shot smal sonemady someone sul store struggling suppies suprosed that the they min this through time we tore training up wan won where who wime with wom won works

## TF, IDF, or TF.IDF?

anty adrain adrian apear apartment apollo ame balboa beoome

 earns oase masy extibition outa outemy beaey fight torgot gazzo gear omaen heavyweight tre jergens uer tonw wase manages match meat mickey named nomes atst padinge paulie pennsyvania pet philadelphia pittance poomoer publialy rocky sells set shark sharp shot shy somebody someone stallion store struggling stunt supplies supposed surprised thanksgiving think thrilled time title touting trainer training triumph up ve viciousness visits where who willing won works

## TF, IDF, or TF.IDF?

ability adrain adirian aready apollo aspiring balboa beat befriended befriends boxer boxes boxing canvas cash champion checks chooses collecting collector creed current deadbeats debt debts distance doesn downtown earns ease easily exhibition explains extra extremely factory - forgot gazzo gear giving gotten heavyweight ddea interested Hatian jergens mom loan ot tovers managers math meat mickey nobody odds packing paulie pennsylvania pet philadelphia pittance promoter prove publicity ready rocky sells shark sharp shop shy skils Somebody spends stallion strugging stunt supplies supposed surprised thanksgiving think thrilled tute touting trainer trainng triumph unkrown ve viciousness visist ... wiling win won

## Queries as TF.IDF Vectors

- Terms tend to appear only once in the query
- TF usually equals 1
- IDF is computed using the collection statistics

$$
i d f_{t}=\log \left(\frac{N}{d f_{t}}\right)
$$

- Terms appearing in fewer documents get a higher weight


## Queries as TF.IDF Vectors

examples from $A O L$ queries with clicks on IMDB results

| term I | tf.idf | term 2 | tf.idf | term 3 | tf.idf |
| :---: | :---: | :---: | :---: | :---: | :---: |
| central | 4.89 | casting | 6.05 | ny | 5.99 |
| wizard | 6.04 | of | 0.18 | oz | 6.14 |
| sam | 2.80 | jones | 3.15 | iii | 2.26 |
| film | 2.31 | technical | 6.34 | advisors | 8.74 |
| edie | 7.41 | sands | 5.88 | singer | 3.88 |
| high | 3.09 | fidelity | 7.66 | quotes | 8.11 |
| quotes | 8.11 | about | 1.61 | brides | 6.71 |
| title | 4.71 | wave | 5.68 | pics | 10.96 |
| saw | 4.87 | 3 | 2.43 | trailers | 7.83 |
| the | 0.03 | rainmaker | 9.09 | movie | 0.00 |
| nancy | 5.50 | and | 0.09 | sluggo | 9.46 |
| audrey | 6.30 | rose | 4.52 | movie | 0.00 |
| mark | 2.43 | sway | 7.53 | photo | 5.14 |
| piece | 4.59 | of | 0.18 | cheese | 6.38 |
| date | 3.93 | movie | 0.00 | cast | 0.00 |

## Vector Space Model

 cosine similarity example (tf.idf weights)$$
\frac{\sum_{i=1}^{V} x_{i} \times y_{i}}{\sqrt{\sum_{i=1}^{V} x_{i}^{2}} \times \sqrt{\sum_{i=1}^{V} y_{i}^{2}}}
$$

$\operatorname{cosine}([2.3,0.0,1.5],[5.4,2.0,0.0])=$

$$
\frac{(2.3 \times 5.4)+(0.0 \times 2.0)+(1.5 \times 0.0)}{\sqrt{2.3^{2}+0.0^{2}+1.5^{2}} \times \sqrt{5.4^{2}+2.0^{2}+0.0^{2}}}
$$

## Vector Space Model cosine similarity example (tf.idf weights)

- Rank documents based on cosine similarity to the query



## TF.IDF

- Many variants of this formula have been proposed
- However, they all have two components in common:
- TF: favors terms that are frequent in the document
- IDF: favors terms that do not occur in many documents

$$
t f_{t} \times \log \left(\frac{N}{d f_{t}}\right)
$$

## Independence Assumption

- The basis vectors ( $\mathbf{X}, \mathbf{Y}, \mathbf{Z}$ ) are linearly independent because knowing a vector's value on one dimension doesn't say anything about its value along another dimension
does this hold true for natural language text?

$$
Y=m a n
$$

basis vectors for 3-dimensional space

## Mutual Information IMDB Corpus

- If this were true, what would these mutual information values be?

| wI | w2 | MI | wI | w2 | MI |
| :---: | :---: | :---: | :---: | :---: | :---: |
| francisco | san | $?$ | dollars | million | $?$ |
| angeles | los | $?$ | brooke | rick | $?$ |
| prime | minister | $?$ | teach | lesson | $?$ |
| united | states | $?$ | canada | canadian | $?$ |
| 9 | II | $?$ | un | ma | $?$ |
| winning | award | $?$ | nicole | roman | $?$ |
| brooke | taylor | $?$ | china | chinese | $?$ |
| con | un | $?$ | japan | japanese | $?$ |
| un | la | $?$ | belle | roman | $?$ |
| belle | nicole | $?$ | border | mexican | $?$ |
| 53 |  |  |  |  |  |

## Mutual Information IMDB Corpus

- These mutual information values should be zero!

| wI | w2 | MI | wl | w2 | MI |
| :---: | :---: | :---: | :---: | :---: | :---: |
| francisco | san | 6.619 | dollars | million | 5.437 |
| angeles | los | 6.282 | brooke | rick | 5.405 |
| prime | minister | 5.976 | teach | lesson | 5.370 |
| united | states | 5.765 | canada | canadian | 5.338 |
| 9 | II | 5.639 | un | ma | 5.334 |
| winning | award | 5.597 | nicole | roman | 5.255 |
| brooke | taylor | 5.518 | china | chinese | 5.231 |
| con | un | 5.514 | japan | japanese | 5.204 |
| un | la | 5.512 | belle | roman | 5.202 |
| belle | nicole | 5.508 | border | mexican | 5.186 |

## Independence Assumption

- The vector space model assumes that terms are independent
- The fact that one occurs says nothing about another one occurring
- This is viewed as a limitation
- However, the implications of this limitation are still debated
- A very popular solution



## Vector Space Model

- Any text can be seen as a vector in V-dimensional space
- a document
- a query
- a sentence
- a word
- an entire encyclopedia
- Rank documents based on their cosine similarity to query
- If a document is similar to the query, it is likely to be relevant (remember: topical relevance!)


## Vector Space Representation

- A power tool!
- A lot of problems in IR can be cast as:
- Find me $\qquad$ that is similar to $\qquad$ !
- As long as ___ and ___ are associated with text, one potential solution is:
- represent these items as tf.idf term-weight vectors and compute their cosine similarity
- return the items with the highest similarity


## Vector Space Representation

- Find documents that are similar to this query


## apple ipad

```
Apple - iPad 2 - All-new design. Video calls. HD video. And more. www.apple.com/ipad/ - Cached
All-new thinner, lighter design. Faster A5 chip. FaceTime video calling. With the same 10 -hour battery. It's not a tablet, it's iPad 2. Starts at \(\$ 499\).
```

Buy iPad Now
store.apple.com/us/...ipad/.../ipad
Buy the iPad 2 today. The ...

## Features

www.apple.com/ipad/features/
Two cameras for video calling ...

## Tech Specs

www.apple.com/ipad/specs/
See full tech specs for iPad ...
iPad with Wi-Fi + 3G.
www.apple.com/ipad/3g/
iPad with Wi-Fi +3 G is perfect ...
Guided Tours
www.apple.com/ipad/guided-tours/
Watch the Guided Tours see all ...
From the App Store
www.apple.com/ipad/from-the-app-s...
Discover thousands of new apps ...

More results from apple.com »

## Apple

www.apple.com/ - Cached
Apple designs and creates iPod and iTunes, Mac laptop and desktop computers ...
4,691 people +1 'd this
$\pm$ Show more results from apple.com

## Vector Space Representation

## - Find ads that are similar to these results

## apple ipad

| Apple - iPad 2-All-new design. Video calls. HD video. And more. <br> www.apple.com/ipad/ - Cached <br> All-new thinner, lighter design. Faster A5 chip. FaceTime video calling. With the same 10-hour battery. It's not a tablet, it's iPad 2. Starts at $\$ 499$. |  | Ads |
| :---: | :---: | :---: |
|  |  | iPad On Verizon. On Sale. <br> www.verizonwireless.com/iPad <br> Magic of iPad. Power of Verizon. |
| Buy iPad Now | iPad with $\mathrm{Wi}-\mathrm{Fi}+3 \mathrm{G}$. | Free Shipping With Online Orders |
| store.apple.com/us/...ipad/.../ipad | www.apple.com/ipad/3g/ | 5319 New Hope Commons Ext, Durham |
| Buy the iPad 2 today. The ... | iPad with Wi-Fi + 3G is perfect ... |  |
| Features | Guided Tours | iPad Apple at Amazon |
|  |  | www.amazon.com/iPad+Apple |
| Two cameras for video calling ... | Watch the Guided Tours see all ... |  |
| Tech Specs | From the App Store | Free 2-Day Shipping w/Amazon Prime. |
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## Vector Space Representation

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## What Is Anatidaephobia?

Anatidaephobia is defined as a pervasive, irrational fear that one is being watched by a duck. The anatidaephobic individual fears that no matter where they are or what they are doing, a duck watches.

Anatidaephobia is derived from the Greek word "anatidae", meaning ducks, geese or swans and "phobos"


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meaning fear.

What Causes Anatidaephobia?

As with all phobias, the person coping with Anatidaephobia has experienced a real-life trauma. For the anatidaephobic individual, this trauma most likely occurred during childhood.

Perhaps the individual was intensely frightened by some species of water fowl. Geese and swans are relatively well known for their aggressive tendencies and perhaps the anatidaephobic person was actually bitten or flapped at. Of course, the Far Side comics did little to minimize the fear of

## Vector Space Representation

- Find queries that are similar to this query


## Google

## apple ipad

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## Vector Space Representation

－Topic categorization：automatically assigning a document to a category

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| Games | Health | Home |
| Video Games， ，RPGs，Gambling．．． | Fitness，Medicine，Alternative．．． | Family，Consumers，Cooking．．． |
| Kids and Teens | News | Recreation |
| Arts，School Time，Teen Life．．． | Media，Newspapers，Weather．．． | Travel，Food，Outdoors，Humor．．． |
| Reference | Regional | Science |
| Maps，Education，Libraries．．． | US，Canada，UK，Europe．．． | Biology，Psychology Physics．．． |
| Shopping | Society | Sports |
| Clothing，Food，Gifts．．． | People，Religion，Issues．．． | Bascball，Soccer，Basketball．．． |
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## Vector Space Representation

- Find documents (with a known category assignment) that are similar to this document

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The Free Encyclopedia

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Article Discussion

## Gerard Salton

From Wikipedia, the free encyclopedia
Gerard Salton (8 March 1927 in Nuremberg - 28 August 1995), also known as Gerry Salton, was a Professor of Computer Science at Comell University. Salton was perhaps the leading computer scientist working in the field of information retrieval during his time. His group at Cornell developed the SMART Information Retrieval System, which he initiated when he was at Harvard.

Salton was born Gerhard Anton Sahimann on March 8, 1927 in Nuremberg, Germany. He received a Bachelor's (1950) and Master's (1952) degree in mathematics from Brooklyn College, and a Ph.D. from Harvard in Applied Mathematics in 1958, the last of Howard Aiken's doctoral students, and taught there until 1965, when he joined Cornell University and co-founded its department of Computer Science.

Salton was perhaps most well known for developing the now widely used Vector Space Model for Information Retrieval ${ }^{\text {[1] }}$. In this model, both documents and queries are represented as vectors of term counts, and the similarity between a document and a query is given by the cosine between the term vector and the document vector. In this paper, he also introduced TF-IDF, or term-frequency-inverse-document frequency, a model in which the score of a term in the a document is the ratio of the number of terms in that document divided by the frequency of the number of documents in which that term occurs. (The concept of inverse document frequency, a measure of specificity, had been introduced in 1972 by Karen Sparck-Jones ${ }^{[2]}$.) Later in life, he became interested in automatic text summarization and analysis ${ }^{[3]}$, as well as automatic hypertext generation ${ }^{[4]}$. He published over 150 research articles and 5 books during his life

Salton was editor-in-chief of the Communications of the ACM and the Journal of the ACM, and chaired SIGIR. He was an associate editor of the ACM Transactions on Information Systems. He was an ACM Fellow (elected 1995), received an Award of Merit from the American Society for Information Science (1989), and was the first recipient of the SIGIR Award for outstanding contributions to study of information retrieval (1983) -- now called the Gerard Salton Award.
advanced

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Internet, Software, Hardware...
Home
Family, Consumers, Cooking...
Recreation
Travel, Food, Outdoors, Humor...
Science
Biology, Psychology, Physics...

## Sports

Baseball, Soccer, Basketball...
ands, Polski, Pyccкий, Svenska...

## Vector Space Representation

- Find documents (with a known category assignment) that are similar to this document



## Summary

- Any text can be seen as a vector in V-dimensional space
- a document
- a query
- a sentence
- a word
- an entire encyclopedia
- Rank documents based on their cosine similarity to query
- If a document is similar to the query, it is likely to be relevant (remember: topical relevance!)

